

Blockchain Decalogue

What Would Wei Wu Say on Blockchain

区块链津逮：十堂公开课与一首无止境的技术诗

 AlphaWallet ×  网易云课堂

Oct 18 ~ Nov 29, Weekly on every Thursday, 18:30 PM
PayPal Lab, Singapore



Talk 1: Elliptic curve and what was achieved before blockchain

Ask yourself, which of the following are unique to blockchain?

- a) integrity (data can be tested against changes).
- b) authenticity (only the keyholder could have done it).
- c) Non-repudiation (undeniable proof);

Jesus told John, "I know what is right. And I would like you to baptize me." So John dipped Jesus into the flowing river. Then the Spirit of God came down and rested on Jesus.



Question: why blockchain was so innovative?

Answer: because a lot of prior work was done before its conception...

Properties of a digital signature scheme

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- c) Non-repudiation (the keyholder couldn't deny having done it);

Please wait a minute our support staff will be

online. Please wait a minute our support staff will be

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Alice: Hi how can I help you today.

Bob: I wish to change my number to a new SIM card. The card number is Bob: I

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8972837283748273381.8972837283748273381.

Alice: Great I can certainly help you with that. Can you tell me your name, Alice:

Great I can certainly help you with that. Can you tell me your name,

date of birth and your support code?date of birth and your support

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Alice: Perfect. Thank you Mr Boon. Your number is transferred to the new Alice:

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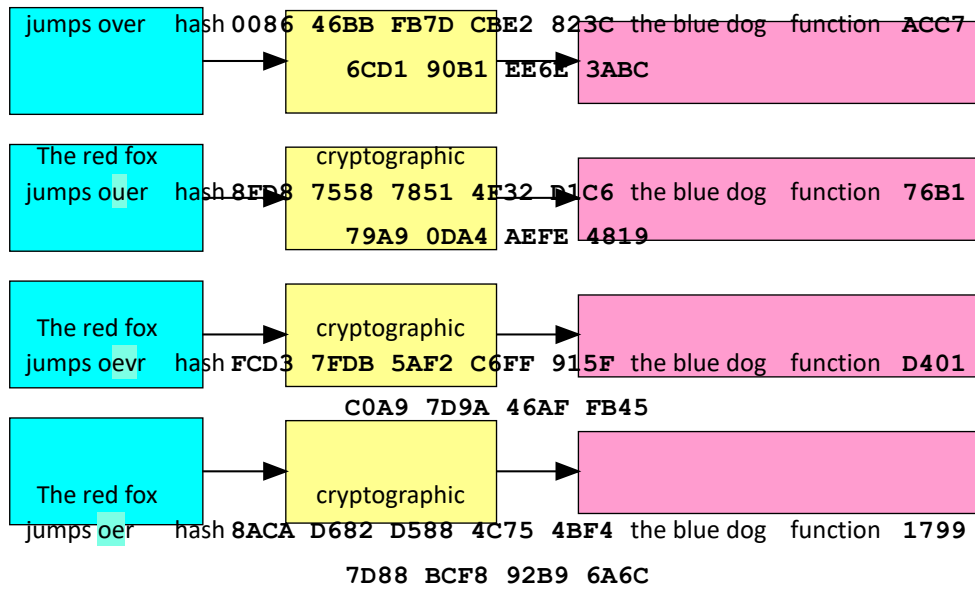
Bob: That's all good thanks!Bob: That's all good thanks!

Alice: Have a nice day! Please rate my service from 1 to 5.Alice: Have a nice day!
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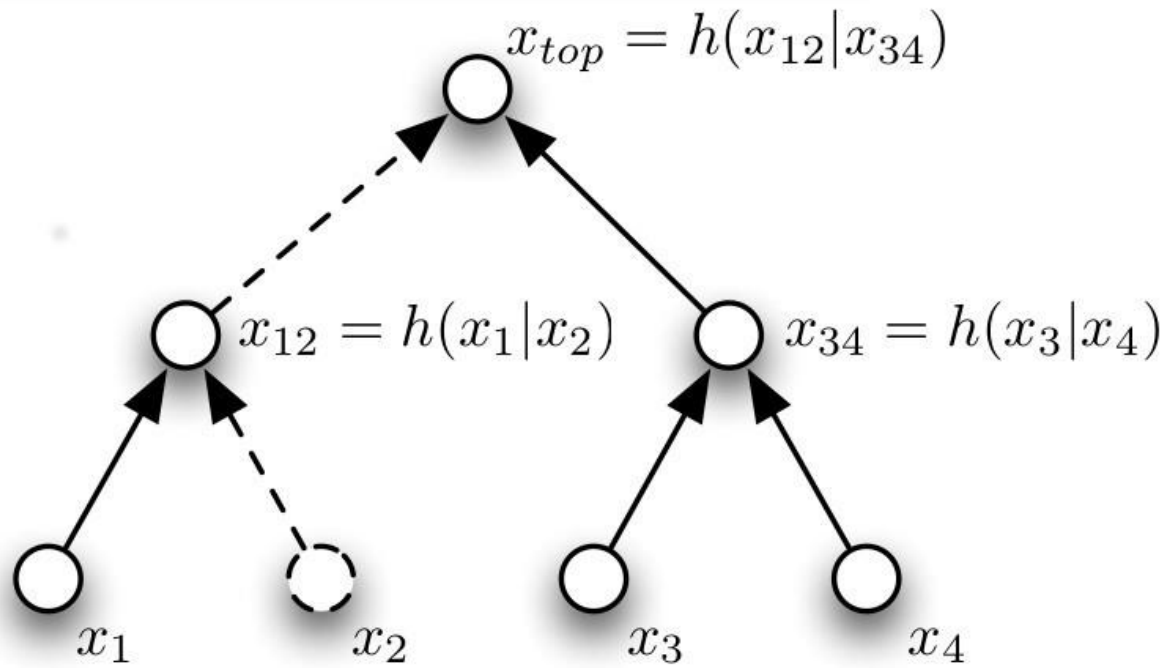
[Bob left the conversation[Bob left the conversation]]

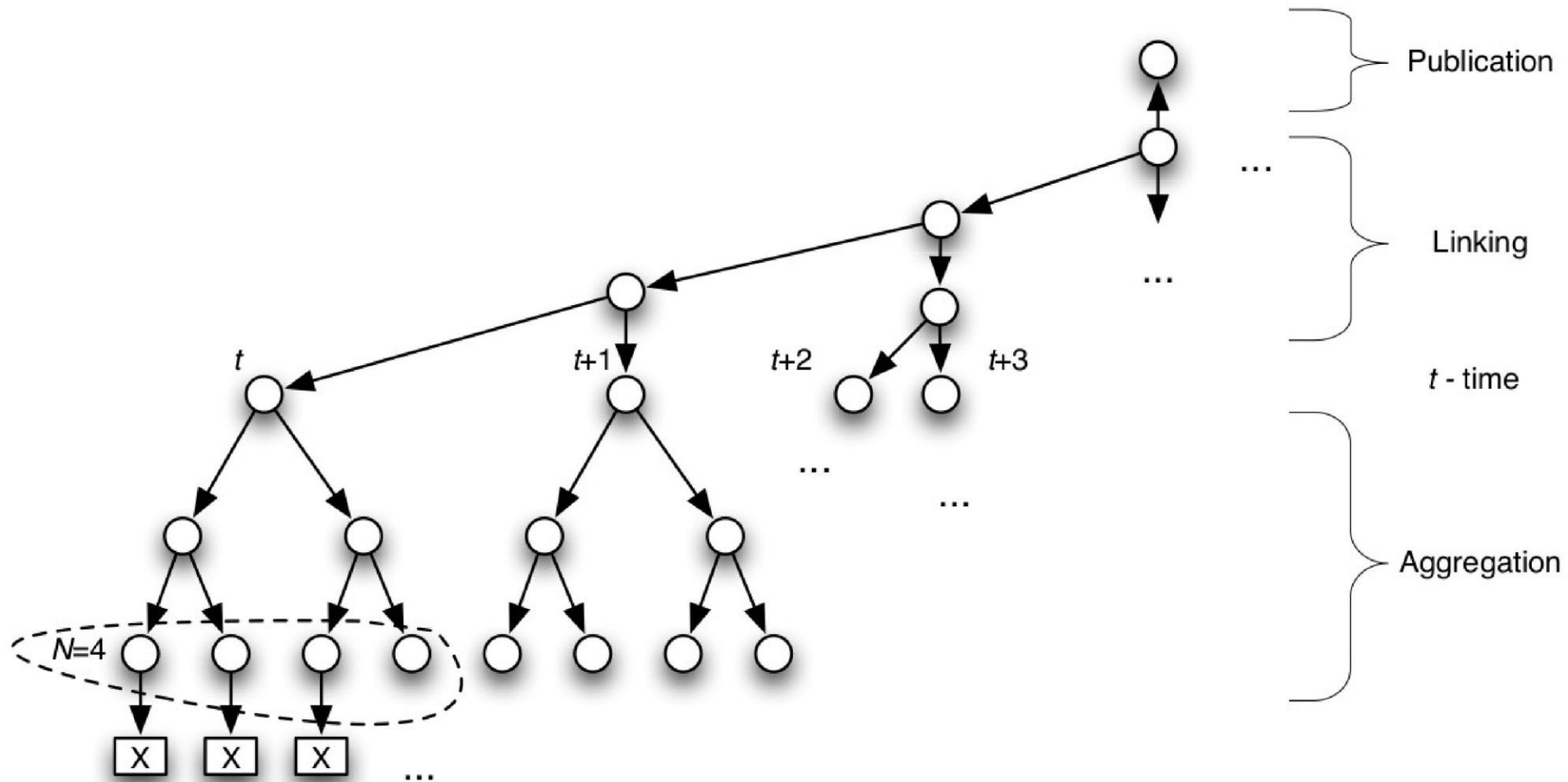
Data integrity 1: Hash Function

Input		Digest
Fox	cryptographic hash function	DFCD 3454 BBEA 788A 751A 696C 24D9 7009 CA99 2D17
The red fox	cryptographic	



https://en.wikipedia.org/wiki/File:Cryptographic_Hash_Function.svg





**A ladder approach
to one way function
and hash function**



Jacob's Dream, 1705, James Thornhill



38742

0489=

x^x



We're here

Message to be hashed

```
$ echo -n "I love Singapore." | xxd -p
```

```
49206C6F76652053696E6761706F72652E
```

```
$ dc -e '16 i 9 o 49206C6F76652053696E6761706F72652E p'
```

```
2063135486757217276684275754075168713178626
```

```
$ dc -e '16 i 4 o 49206C6F76652053696E6761706F72652E p' | tr '0123'
'\+\-\*\\/'
```

```
-+*-+*+--*/+-*//--/*--*--++---+/-**--*/*-*/-*/-*/-*/-*/-
/*-*/-+*/$ dc -e '4 2-6+6*7-6+2+5*6+6+6-6*7/6+7-
6*2/20/54-72/66-57*51-31*6/p'
```

```
-19700$
```

Message to be hashed

```
$ echo -n "I love S'pore." | xxd -p
```

```
4920686F74652053E28099706F72652E
```

```
$ dc -e '16i 9o 4920686F74652053E28099706F72652E p'
```

```
5823566860642002606306862507646714474542
```

```
$ dc -e '16i 4o 4920686F74652053E28099706F72652E p' | tr '0123'
'\+\-\*\\/'
```

```
-$ dc -e '4 2-6+6*7-6+2/E+8-9*7*6-7*6/2/68/20-63+25-
```

```
$ bc <<< 'g=5; q=277; for (i=1; i<q; i++) {g^i%q}' | uniq -c | column -c 250 | sed
's/\t */\t/g' | expand -t6
```



```

1 135 1 207 1 262 1 254 1 94 1 218 1 205 1 222 1 8 1 160 1 153 1 13 1 260 1
214
1 121 1 204 1 202 1 162 1 193 1 259 1 194 1 2 1 40 1 246 1 211 1 65 1 192 1
239
1 51 1 189 1 179 1 256 1 134 1 187 1 139 1 10 1 200 1 122 1 224 1 48 1 129 1
87
1 255 1 114 1 64 1 172 1 116 1 104 1 141 1 50 1 169 1 56 1 12 1 240 1 91 1
158
1 167 1 16 1 43 1 29 1 26 1 243 1 151 1 250 1 14 1 3 1 60 1 92 1 178 1
236
1 4 1 80 1 215 1 145 1 130 1 107 1 201 1 142 1 70 1 15 1 23 1 183 1 59 1
72
1 20 1 123 1 244 1 171 1 96 1 258 1 174 1 156 1 73 1 75 1 115 1 84 1 18 1

```

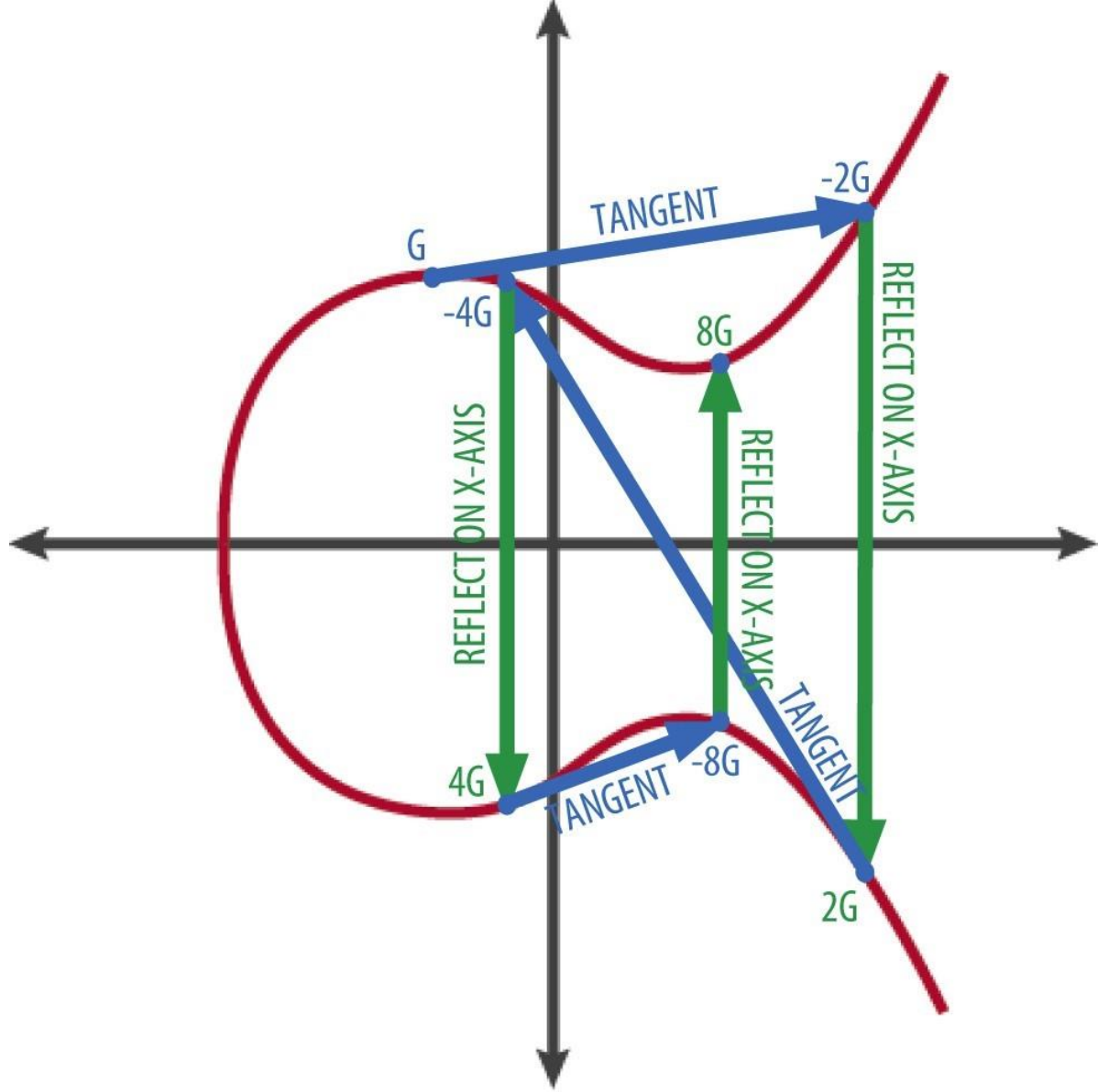
```

$ bc <<< 'g=5; q=277; for (i=1; i<q; i++) {g^i%q}' | sort -n| uniq -c | column -c 250
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1 1 1 20 1 39 1 58 1 77 1 96 1 115 1 134 1 153 1 172 1 191 1 210 1 229 1
248 1 267
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249 1 268
1 3 1 22 1 41 1 60 1 79 1 98 1 117 1 136 1 155 1 174 1 193 1 212 1 231 1
250 1 269
1 4 1 23 1 42 1 61 1 80 1 99 1 118 1 137 1 156 1 175 1 194 1 213 1 232 1
251 1 270

```

252	1 5	1 24	1 43	1 62	1 81	1 100	1 119	1 138	1 157	1 176	1 195	1 214	1 233	1
	1 271													
253	1 6	1 25	1 44	1 63	1 82	1 101	1 120	1 139	1 158	1 177	1 196	1 215	1 234	1
	1 272													
254	1 7	1 26	1 45	1 64	1 83	1 102	1 121	1 140	1 159	1 178	1 197	1 216	1 235	1
	1 273													
255	1 8	1 27	1 46	1 65	1 84	1 103	1 122	1 141	1 160	1 179	1 198	1 217	1 236	1
	1 274													
256	1 9	1 28	1 47	1 66	1 85	1 104	1 123	1 142	1 161	1 180	1 199	1 218	1 237	1
	1 275													
257	1 10	1 29	1 48	1 67	1 86	1 105	1 124	1 143	1 162	1 181	1 200	1 219	1 238	1
	1 276													
258	1 11	1 30	1 49	1 68	1 87	1 106	1 125	1 144	1 163	1 182	1 201	1 220	1 239	1
259	1 12	1 31	1 50	1 69	1 88	1 107	1 126	1 145	1 164	1 183	1 202	1 221	1 240	1
260	1 13	1 32	1 51	1 70	1 89	1 108	1 127	1 146	1 165	1 184	1 203	1 222	1 241	1
261	1 14	1 33	1 52	1 71	1 90	1 109	1 128	1 147	1 166	1 185	1 204	1 223	1 242	1
262	1 15	1 34	1 53	1 72	1 91	1 110	1 129	1 148	1 167	1 186	1 205	1 224	1 243	1
263	1 16	1 35	1 54	1 73	1 92	1 111	1 130	1 149	1 168	1 187	1 206	1 225	1 244	1

264	1	17	1	36	1	55	1	74	1	93	1	112	1	131	1	150	1	169	1	188	1	207	1	226	1	245	1
265	1	18	1	37	1	56	1	75	1	94	1	113	1	132	1	151	1	170	1	189	1	208	1	227	1	246	1
266	1	19	1	38	1	57	1	76	1	95	1	114	1	133	1	152	1	171	1	190	1	209	1	228	1	247	1



Schnorr Signature

- Signing

- Let $r = g^k$
- Let $e = H(r || M) = H(g^k || M)$
- Let $s = k - xe$
 $xe = H(r || M)$
- The signature is $(r, s = k - xe)$

- Verify

- Let $r = g^k_v = g^s y^{ee}$
- Let $e = H(r || M)_v = H(g^k_v || M)$
- If $e = H(r || M)_v = e = H(r || M)$
the signature is valid.

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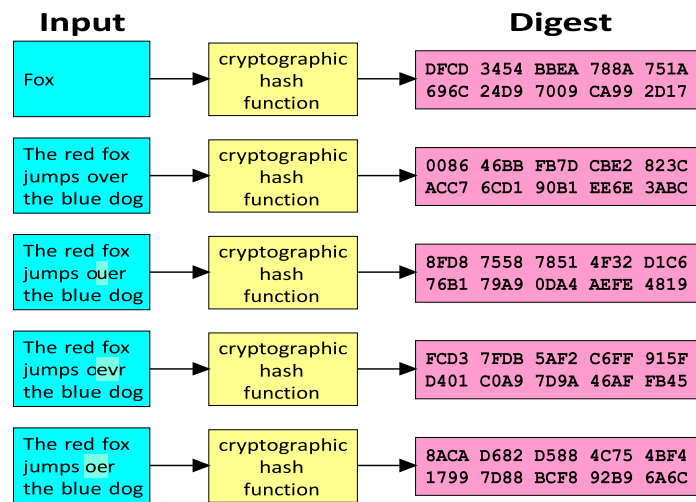
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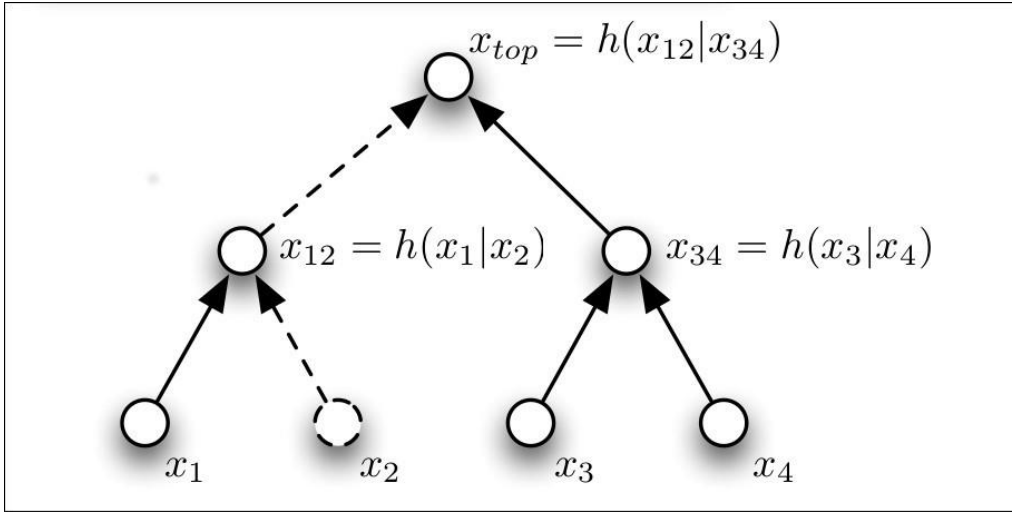
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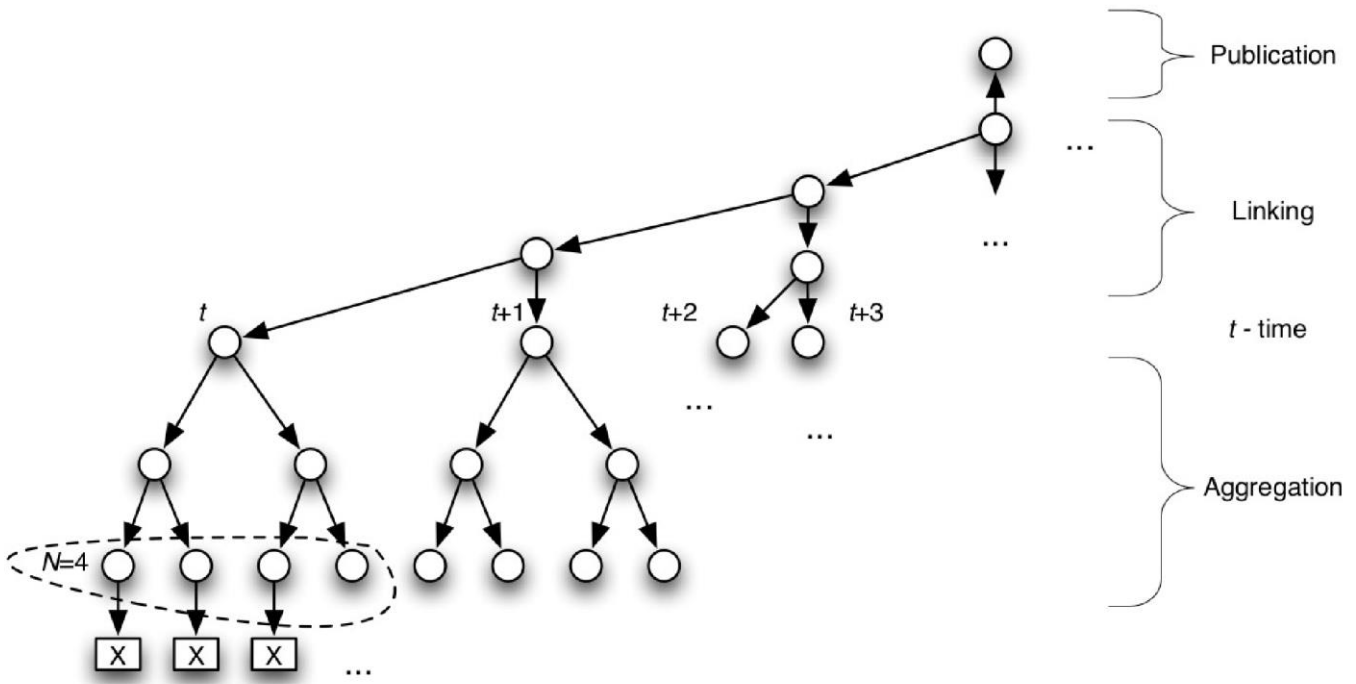
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https://en.wikipedia.org/wiki/File:Cryptographic_Hash_Function.svg





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Jacob's Dream, 1705, James Thornhill

387420489 = x^x



We're here

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49206C6F76652053696E6761706F72652E  
$ dc -e '16 i 9 o 49206C6F76652053696E6761706F72652E p'  
2063135486757217276684275754075168713178626  
$ dc -e '16 i 4 o 49206C6F76652053696E6761706F72652E p' | tr '0123'  
'\+\-\*\\/'  
-+*-+*+-*/+*//-/--*-*-++*+---+/-**--*/*-*/-+*---/++-*/-  
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6*2/20/54-72/66-57*51-31*6/p'
```

-19700\$

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4920686F74652053E28099706F72652E  
$ dc -e '16i 9o 4920686F74652053E28099706F72652E p'  
5823566860642002606306862507646714474542  
$ dc -e '16i 4o 4920686F74652053E28099706F72652E p' | tr '0123'  
'\+\-\*\\/'  
-+*-+*+-**+*//-/++*---+*+---+//**+*+*+*+*---/++-*/-/+*-*---+*/
```

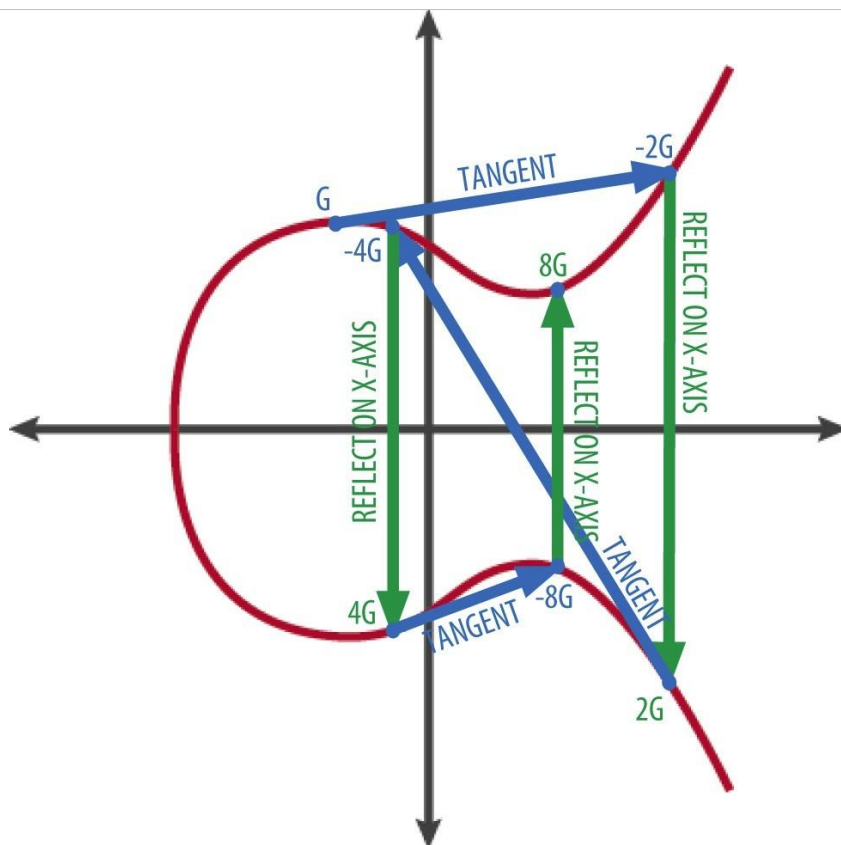
\$ dc -e '4 2-6+6*7-6+2*5+E+8-9*7*6-7*6/2/58-68/20-63+25-
67*45-p' 4846

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1 90 1 138
  1 25 1 223 1 28 1 6 1 120 1 184 1 79 1 195 1 22 1 163 1 213 1 105 1 161
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1 34 1 126
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1 19 1 103
  1 113 1 44 1 49 1 149 1 210 1 45 1 69 1 272 1 177 1 216 1 165 1 253 1 74
1 95 1 238
  1 11 1 220 1 245 1 191 1 219 1 225 1 68 1 252 1 54 1 249 1 271 1 157 1 93
1 198 1 82
  1 55 1 269 1 117 1 124 1 264 1 17 1 63 1 152 1 270 1 137 1 247 1 231 1 188
1 159 1 133
  1 275 1 237 1 31 1 66 1 212 1 85 1 38 1 206 1 242 1 131 1 127 1 47 1 109
1 241 1 111
  1 267 1 77 1 155 1 53 1 200 1 140 1 100 1 100 1 100 1 101 1 01 1 225 1 260
1 97 1 1
  1 227 1 108 1 221 1 265 1 27 1 106 1 110 1 164 1 22 1 228 1 128 1 67 1 232
1 208
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1 27 1 263 1 274 1 217 1 185 1 99 1 41 1 266 1 57 1 32 1 86 1 58 1 52
1 209
1 135 1 207 1 262 1 254 1 94 1 218 1 205 1 222 1 8 1 160 1 153 1 13 1 260
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  1 11 1 30 1 49 1 68 1 87 1 106 1 125 1 144 1 163 1 182 1 201 1 220 1 239
1 258
```

1 12 1 31 1 50 1 69 1 88 1 107 1 126 1 145 1 164 1 183 1 202 1 221 1 240
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1 17 1 36 1 55 1 74 1 93 1 112 1 131 1 150 1 169 1 188 1 207 1 226 1 245
1 264
1 18 1 37 1 56 1 75 1 94 1 113 1 132 1 151 1 170 1 189 1 208 1 227 1 246
1 265
1 19 1 38 1 57 1 76 1 95 1 114 1 133 1 152 1 171 1 190 1 209 1 228 1 247
1 266



Schnorr Signature

• Signing

$$- \text{Let } r = g^k$$

$$- \text{Let } e = H(r || M) = H(g^k || M)$$

$$- \text{Let } s = k - xe \quad \text{where } x = e^{-1} \text{ mod } q$$

• Verify

$$- \text{Let } r = g^k_v = g^s y^{ee}$$

$$- \text{Let } e = H(r || M)_v = H(g^s y^{ee} || M)$$

$$- \text{If } e = H(r || M)_v = e = H(r || M)$$

- The signature is $(r, s = k^{-1}(e + H(r || M)))$ the signature is valid.

